

Adding and Subtracting Polynomials

Simplify each expression.

1) $(5p^2 - 3) + (2p^2 - 3p^3)$
 $-3p^3 + 7p^2 - 3$

2) $(a^3 - 2a^2) - (3a^2 - 4a^3)$
 $5a^3 - 5a^2$

3) $(4 + 2n^3) + (5n^3 + 2)$
 $7n^3 + 6$

4) $(4n - 3n^3) - (3n^3 + 4n)$
 $-6n^3$

5) $(3a^2 + 1) - (4 + 2a^2)$
 $a^2 - 3$

6) $(4r^3 + 3r^4) - (r^4 - 5r^3)$
 $2r^4 + 9r^3$

7) $(5a + 4) - (5a + 3)$
 1

8) $(3x^4 - 3x) - (3x - 3x^4)$
 $6x^4 - 6x$

9) $(-4k^4 + 14 + 3k^2) + (-3k^4 - 14k^2 - 8)$
 $-7k^4 - 11k^2 + 6$

10) $(3 - 6n^5 - 8n^4) - (-6n^4 - 3n - 8n^5)$
 $2n^5 - 2n^4 + 3n + 3$

11) $(12a^5 - 6a - 10a^3) - (10a - 2a^5 - 14a^4)$
 $14a^5 + 14a^4 - 10a^3 - 16a$

12) $(8n - 3n^4 + 10n^2) - (3n^2 + 11n^4 - 7)$
 $-14n^4 + 7n^2 + 8n + 7$

13) $(-x^4 + 13x^5 + 6x^3) + (6x^3 + 5x^5 + 7x^4)$
 $18x^5 + 6x^4 + 12x^3$

14) $(9r^3 + 5r^2 + 11r) + (-2r^3 + 9r - 8r^2)$
 $7r^3 - 3r^2 + 20r$

15) $(13n^2 + 11n - 2n^4) + (-13n^2 - 3n - 6n^4)$
 $-8n^4 + 8n$

16) $(-7x^5 + 14 - 2x) + (10x^4 + 7x + 5x^5)$
 $-2x^5 + 10x^4 + 5x + 14$

$$17) (7 - 13x^3 - 11x) - (2x^3 + 8 - 4x^5)$$
$$4x^5 - 15x^3 - 11x - 1$$

$$18) (13a^2 - 6a^5 - 2a) - (-10a^2 - 11a^5 + 9a)$$
$$5a^5 + 23a^2 - 11a$$

$$19) (3v^5 + 8v^3 - 10v^2) - (-12v^5 + 4v^3 + 14v^2)$$
$$15v^5 + 4v^3 - 24v^2$$

$$20) (8b^3 - 6 + 3b^4) - (b^4 - 7b^3 - 3)$$
$$2b^4 + 15b^3 - 3$$

$$21) (k^4 - 3 - 3k^3) + (-5k^4 + 6k^3 - 8k^5)$$
$$-8k^5 - 4k^4 + 3k^3 - 3$$

$$22) (-10k^2 + 7k + 6k^4) + (-14 - 4k^4 - 14k)$$
$$2k^4 - 10k^2 - 7k - 14$$

$$23) (-7n^2 + 8n - 4) - (-11n + 2 - 14n^2)$$
$$7n^2 + 19n - 6$$

$$24) (14p^4 + 11p^2 - 9p^5) - (-14 + 5p^5 - 11p^2)$$
$$-14p^5 + 14p^4 + 22p^2 + 14$$

$$25) (8k + k^2 - 6) - (-10k + 7 - 2k^2)$$
$$3k^2 + 18k - 13$$

$$26) (-9v^2 - 8u) + (-2uv - 2u^2 + v^2) + (-v^2 + 4uv)$$
$$-9v^2 + 2uv - 2u^2 - 8u$$

$$27) (4x^2 + 7x^3y^2) - (-6x^2 - 7x^3y^2 - 4x) - (10x + 9x^2)$$
$$14x^3y^2 + x^2 - 6x$$

$$28) (-5u^3v^4 + 9u) + (-5u^3v^4 - 8u + 8u^2v^2) + (-8u^4v^2 + 8u^3v^4)$$
$$-2u^3v^4 - 8u^4v^2 + 8u^2v^2 + u$$

$$29) (-9xy^3 - 9x^4y^3) + (3xy^3 + 7y^4 - 8x^4y^4) + (3x^4y^3 + 2xy^3)$$
$$-8x^4y^4 - 6x^4y^3 + 7y^4 - 4xy^3$$

$$30) (y^3 - 7x^4y^4) + (-10x^4y^3 + 6y^3 + 4x^4y^4) - (x^4y^3 + 6x^4y^4)$$
$$-9x^4y^4 - 11x^4y^3 + 7y^3$$

Multiplying Polynomials**Find each product.**

1) $6v(2v + 3)$

$$12v^2 + 18v$$

2) $7(-5v - 8)$

$$-35v - 56$$

3) $2x(-2x - 3)$

$$-4x^2 - 6x$$

4) $-4(v + 1)$

$$-4v - 4$$

5) $(2n + 2)(6n + 1)$

$$12n^2 + 14n + 2$$

6) $(4n + 1)(2n + 6)$

$$8n^2 + 26n + 6$$

7) $(x - 3)(6x - 2)$

$$6x^2 - 20x + 6$$

8) $(8p - 2)(6p + 2)$

$$48p^2 + 4p - 4$$

9) $(6p + 8)(5p - 8)$

$$30p^2 - 8p - 64$$

10) $(3m - 1)(8m + 7)$

$$24m^2 + 13m - 7$$

11) $(2a - 1)(8a - 5)$

$$16a^2 - 18a + 5$$

12) $(5n + 6)(5n - 5)$

$$25n^2 + 5n - 30$$

$$13) \ (4p - 1)^2$$
$$16p^2 - 8p + 1$$

$$14) \ (7x - 6)(5x + 6)$$
$$35x^2 + 12x - 36$$

$$15) \ (6n + 3)(6n - 4)$$
$$36n^2 - 6n - 12$$

$$16) \ (8n + 1)(6n - 3)$$
$$48n^2 - 18n - 3$$

$$17) \ (6k + 5)(5k + 5)$$
$$30k^2 + 55k + 25$$

$$18) \ (3x - 4)(4x + 3)$$
$$12x^2 - 7x - 12$$

$$19) \ (4a + 2)(6a^2 - a + 2)$$
$$24a^3 + 8a^2 + 6a + 4$$

$$20) \ (7k - 3)(k^2 - 2k + 7)$$
$$7k^3 - 17k^2 + 55k - 21$$

$$21) \ (7r^2 - 6r - 6)(2r - 4)$$
$$14r^3 - 40r^2 + 12r + 24$$

$$22) \ (n^2 + 6n - 4)(2n - 4)$$
$$2n^3 + 8n^2 - 32n + 16$$

$$23) \ (6n^2 - 6n - 5)(7n^2 + 6n - 5)$$
$$42n^4 - 6n^3 - 101n^2 + 25$$

7-4 Study Guide and Intervention (continued)

Polynomials

Write Polynomials in Standard Form The terms of a polynomial are usually arranged so that the terms are in order from greatest degree to least degree. This is called the **standard form** of a polynomial.

Example Write $-4x^3 + 8x^4 - 2x$ in standard form. Identify the leading coefficient.

Step 1: Find the degree of each term.

Polynomial: $-4x^3 + 8x^4 - 2x$

Degree: $\begin{array}{c} 3 \\ 4 \\ 1 \end{array}$

Step 2: Write the terms in descending order: $8x^4 - 4x^3 - 2x$.

The leading coefficient is 9.

Exercises

Write each polynomial in standard form. Identify the leading coefficient.

1. $5x + x^2 + 6$ $2. 6x + 9 - 4x^2$ $3. x^4 + x^3 + x^2$

$$\underline{x^2 + 5x + 6; 1}$$

$$\underline{-4x^2 + 6x + 9; -4}$$

$$\quad\quad\quad x^4 + x^3 + x^2; 1$$

4. $2x^2 - x + 3x^7$ $5. 2x + x^2 - 5$ $6. 20x - 10x^2 + 5x^3$

$$\underline{3x^7 + 2x^3 - 7; 3}$$

$$\underline{x^2 + 2x - 5; 1}$$

$$\underline{5x^3 - 10x^2 + 20x; 5}$$

7. $x^2 + x^4 - x^2$ $8. x^4 + 4x^3 + 5$ $9. -3x^4 - x^5 + 2x^3$

$$\underline{x^5 + x^3 - x^2; 1}$$

$$\underline{-7x^6 + x^4 + 4x^3 + 1; -7}$$

$$\quad\quad\quad 2x^6 - 3x^4 - x^5; 2$$

10. $2x^7 - x^8$ $11. 3x + 5x^4 - 2 - x^2$ $12. -2x^4 + x - 4x^5 + 3$

$$\underline{-x^8 + 2x^7; -1}$$

$$\underline{5x^4 - x^2 + 3x - 2; 5}$$

$$\quad\quad\quad -4x^6 - 2x^4 + x + 3; -4$$

13. $2 - x^3$ $14. 5x^4 - 12x - 3x^6$ $15. 9x^7 - 9 + 3x^3 - 6x^6$

$$\underline{-x^6 + 5x^4 - 12x; -1}$$

$$\quad\quad\quad -3x^6 + 5x^4 - 12x; -3$$

$$\quad\quad\quad 9x^7 - 6x^6 + 3x^3 - 9; 9$$

16. $9x^8 - 9 + 3x^3 - 6x^6$ $17. x^3 + 3x^5 + 27 - x$ $18. 25 - x^2 + x$

$$\quad\quad\quad 9x^7 - 6x^6 + 3x^3 - 9; 9$$

$$\underline{5x^8 - x^6 - 2x^4 + x + 3; -4}$$

$$\quad\quad\quad 3x^3 + x^2 - x + 27; 3$$

$$\quad\quad\quad -x^3 + x + 25; -1$$

19. $x - 3x^2 + 4 + 5x^3$ $20. x^2 + 64 - x + 7x^3$ $21. 6x^3 - 7x^5 + x - 2x^4 + 1$

$$\underline{5x^3 - 3x^2 + x + 4; 5}$$

$$\quad\quad\quad -7x^6 + 6x^3 - 2x^2 + x + 1; -7$$

$$\quad\quad\quad -7x^5 + x^3 - x + 64; 7$$

22. $4 - x + 3x^2 - 2x^3$ $23. 13 - 4x^9 + x^3$ $24. 17x^6 - 6x^{10} + 2$

$$\underline{3x^3 - 2x^2 - x + 4; 3}$$

$$\quad\quad\quad -4x^6 + x^3 + 13; -4$$

$$\quad\quad\quad -5x^{17} + 17x^6 + 2; -5$$

Answers (Lesson 7-4)

Lesson 7-4

NAME _____ DATE _____ PERIOD _____

7-4 Skills Practice

Polynomials

Determine whether each expression is a polynomial. If so, identify the polynomial as a **monomial**, **binomial**, or **trinomial**.

1. $5mt + t^2$ 2. $4by + 2b - by$

$$\quad\quad\quad$$

yes; binomial

4. $\frac{3x}{7}$

yes; monomial

6. $2c^4 + 8c + 9 - 3$

yes; trinomial

5. $5x^3 - 3x^{-1}$

no

Find the degree of each polynomial.

7. 120

8. $3r^4 - 4$

9. $b + 61$

10. $4x^8 - 2x - 3$

11. $5abc - 2b^4 + 1; 3$

12. $8x^5y^4 - 2x^2 - 9$

Write each polynomial in standard form. Identify the leading coefficient.

13. $3x + 1 + 2x^2$ 14. $5x - 6 + 3x^2$

$$\underline{2x^2 + 3x + 1; 3}$$

$$\underline{3x^2 + 5x - 6; 3}$$

15. $8x^2 + 2 + x^3 + x$ 16. $-3 + 3x^3 - x^2 + 4x$

$$\underline{x^3 + 9x^2 + x + 2; 1}$$

$$\underline{3x^3 - x^2 + 4x - 3; 3}$$

17. $x^3 + 3x^5 + 27 - x$ 18. $25 - x^2 + x$

$$\underline{3x^3 + x^2 - x + 27; 3}$$

$$\quad\quad\quad -x^3 + x + 25; -1$$

19. $x - 3x^2 + 4 + 5x^3$ 20. $x^2 + 64 - x + 7x^3$

$$\underline{5x^3 - 3x^2 + x + 4; 5}$$

$$\quad\quad\quad -7x^6 + 6x^3 - x + 64; 7$$

21. $6x^3 - 7x^5 + x - 2x^4 + 1$ 22. $4 - x + 3x^2 - 2x^3$

$$\underline{-7x^5 + x^3 - x + 64; 7}$$

$$\quad\quad\quad -7x^6 + 6x^3 - x + 4; 3$$

23. $13 - 4x^9 + x^3$ 24. $17x^6 - 6x^{10} + 2$

$$\underline{-4x^6 + x^3 + 13; -4}$$

$$\quad\quad\quad -5x^{17} + 17x^6 + 2; -5$$

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